

**WHAT IS CLAIMED IS:**

1. A method for designing a vehicle suspension system, comprising:
  - formalizing the vehicle suspension system by an equation (1), the vehicle suspension system including a plurality of springs, a plurality of dampers each corresponding to one of the springs, and a plurality p of actuators, equation (1) being a linear matrix equation having a number, n, degrees of freedom, the linear matrix equation including a damping matrix for viscous damping;
  - calculating eigenvectors of a stiffness matrix  $K$  of equation (1);
  - normalizing the eigenvectors with respect to a mass matrix  $M$  of equation (1);
  - calculating a similarity transform matrix  $S$  consisting of the normalized eigenvectors; and
  - normalizing equation (1) using the similarity transform matrix  $S$ , wherein equation (1) is

$$M\ddot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t)$$

wherein:

n and p respectively denote the degrees of freedom of the suspension system and the number of independent actuators;

$M$ ,  $C$ , and  $K$  respectively denote a mass matrix, a damping matrix, and a stiffness matrix, each of which is symmetrically  $n \times n$ , the mass matrix  $M$  being a positive definite matrix, the damping matrix  $C$  being a positive semi-definite matrix, and the stiffness matrix  $K$  being a positive definite matrix;

$P$  denotes an  $n \times p$  real matrix corresponding to positions of the actuators,

$x(t)$  and  $u(t)$  respectively denote  $n \times 1$  state and disturbance vectors; and

$f(t)$  denotes a  $p \times 1$  external force vector.

2. The method of claim 1, wherein the normalizing equation (1) establishes a proportional relationship  $k_j = \alpha \times c_j$  between each pair of a spring coefficient  $k_j$  of a j-th spring and a damping coefficient  $c_j$  of a j-th damper corresponding to the j-th spring.

3. A vehicle suspension system comprising:  
a plurality of springs;  
a plurality of dampers, each corresponding to one of the springs; and  
a plurality p of actuators for generating control force to the suspension system,

5 wherein:

the suspension system is formalized by an equation (1); and  
equation (1) is decoupled into n modal equations,

wherein equation (1) is a linear matrix equation having a plurality n of degrees of freedom, and the linear matrix equation includes a damping matrix for a viscous damping,

10 wherein equation (1) is

$$M\ddot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t)$$

wherein:

n and p respectively denote the degrees of freedom of the suspension system and  
15 the number of independent actuators;

$M$ ,  $C$ , and  $K$  respectively denote a mass matrix, a damping matrix, and a stiffness matrix, each of which is symmetrically  $n \times n$ , the mass matrix  $M$  being a positive definite matrix, the damping matrix  $C$  being a positive semi-definite matrix, and the stiffness matrix  $K$  being a positive definite matrix;

20  $P$  denotes an  $n \times p$  real matrix corresponding to positions of the actuators,

$x(t)$  and  $u(t)$  respectively denote  $n \times 1$  state and disturbance vectors; and

$f(t)$  denotes  $p \times 1$  external force vector.

4. The vehicle suspension system of claim 3, wherein a proportional relationship  
25  $k_j = \alpha \times c_j$  is satisfied between each pair of a spring coefficient  $k_j$  of a j-th spring and a damping coefficient  $c_j$  of a j-th damper corresponding to the j-th spring.

5. The vehicle suspension system of claim 4, wherein the number n and the  
number p are equal,

30 the suspension system further comprising:

a detecting unit for detecting at least one of the state vector  $x(t)$  and its velocity  $\dot{x}(t)$ ; and

a controller for controlling the actuators on the basis of the detected one of the state vector  $x(t)$  or its velocity  $\dot{x}(t)$ ,

5 wherein the controller controls the actuators by an actuating force of

$$f = Q^{-1} \hat{f},$$

wherein:

$$Q = S^T P, \hat{f}_i = -C_{Si} \dot{\xi}_i, \text{ and } x(t) = S \xi(t) \text{ are satisfied;}$$

$C_{Si}$  is a damping coefficient of a sky-hook damper connected to an i-th mode;

10 and

$S$  is a matrix consisting of eigenvectors of the stiffness matrix  $K$  and is normalized with respect to the mass matrix  $M$ .

6. The vehicle suspension system of claim 4, wherein the number  $p$  is less than the 15 number  $n$ ,

the suspension system further comprising:

a detecting unit for detecting at least one of the state vector  $x(t)$  and its velocity  $\dot{x}(t)$ ; and

a controller for controlling the actuators on the basis of the detected one of the state vector  $x(t)$  or its velocity  $\dot{x}(t)$ ,

20 wherein the controller controls the actuators by an actuating force of

$$\hat{f}_i = -F_{Si} sign(\dot{\xi}_i) = \sum_{j=1}^p Q_{ij} f_j, \\ f(t) \text{ that satisfies}$$

wherein:

$$Q = S^T P \text{ and } x(t) = S \xi(t) \text{ are satisfied;}$$

25  $F_{Si}$  is a frictional force of a sky-hook coulomb friction damper connected to an i-th mode; and

$S$  is a matrix consisting of eigenvectors of the stiffness matrix  $K$  and is normalized with respect to the mass matrix  $M$ .

7. The vehicle suspension system of claim 6, wherein the actuating force  $f(t)$  satisfies

$$\left\{ \begin{array}{ll} \text{if } Q_{1j}\text{sign}(\dot{\xi}_1) \geq 0 \& Q_{2j}\text{sign}(\dot{\xi}_2) \geq 0 \& \cdots Q_{nj}\text{sign}(\dot{\xi}_n) \geq 0, & f_j = -F_A \\ \text{if } Q_{1j}\text{sign}(\dot{\xi}_1) \geq 0 \& Q_{2j}\text{sign}(\dot{\xi}_2) \geq 0 \& \cdots Q_{nj}\text{sign}(\dot{\xi}_n) < 0, & f_j = -F_1 \\ \vdots & \vdots \\ \text{if } Q_{1j}\text{sign}(\dot{\xi}_1) < 0 \& Q_{2j}\text{sign}(\dot{\xi}_2) < 0 \& \cdots Q_{nj}\text{sign}(\dot{\xi}_n) \geq 0, & f_j = -F_{(2^n-2)} \\ \text{if } Q_{1j}\text{sign}(\dot{\xi}_1) < 0 \& Q_{2j}\text{sign}(\dot{\xi}_2) < 0 \& \cdots Q_{nj}\text{sign}(\dot{\xi}_n) < 0, & f_j = -F_B \end{array} \right\}$$

with respect to  $i = 1, \dots, n$  and  $j = 1, \dots, p$ ,

wherein:

$F_A$  is a value in a range of zero(0) to  $F_P$ ;

$F_B$  is a value in a range of zero(0) to  $F_N$ ;

$F_k$  for  $k = 1, \dots, (2^n - 2)$  is a value between  $F_P$  and  $F_N$ ; and

$F_P$  and  $F_N$  respectively denote a positive maximum force and a negative maximum force that a j-th actuator can generate.

15. The vehicle suspension system of claim 7, wherein the actuating force  $f(t)$  satisfies

$$\left\{ \begin{array}{ll} \text{if } Q_{ij}\text{sign}(\dot{\xi}_i) \geq 0 \text{ for } i = 1, \dots, n, & f_j = -F_A \\ \text{if } Q_{ij}\text{sign}(\dot{\xi}_i) < 0 \text{ for } i = 1, \dots, n, & f_j = -F_B \\ \text{Otherwise,} & f_j = 0 \end{array} \right\}$$

with respect to  $i = 1, \dots, n$  and  $j = 1, \dots, p$ .

9. The vehicle suspension system of claim 8, wherein values of  $F_A$  and  $F_P$  are equal, and values of  $F_B$  and  $F_N$  are equal.

10. A method for controlling a vehicle suspension system, the vehicle suspension including a plurality of dampers and a plurality of actuators, the vehicle suspension system being formalized by an equation (1) and being transformed to a decoupled equation (2), the method comprising:

5 calculating a velocity vector  $\dot{x}(t)$  of a state vector  $x(t)$  of equation (1);  
calculating an actuating force  $f(t)$  such that the actuating force  $f(t)$   
10 satisfies  $f(t) = (S^T P)^{-1} (-C_{Si})(S^T K S)^{-1} (S^T K) \dot{x}(t)$ , the  $C_{Si}$  being a damping coefficient of a sky-hook damper connected to an i-th mode; and  
actuating the actuators by the calculated actuating force  $f(t)$ ,

15 wherein:

equation (1) is

$$M\ddot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t), \text{ and}$$

15 equation (2) is

$$I\ddot{\xi}(t) + \text{diag}[2\zeta_i \omega_i](\dot{\xi}(t) - \dot{\eta}(t)) + \Lambda_K(\xi(t) - \eta(t)) = \hat{f}(t)$$

wherein:

n and p respectively denote the degrees of freedom of the suspension system and  
20 the number of independent actuators;

$M$ ,  $C$ , and  $K$  respectively denote a matrix, a damping matrix, and a stiffness matrix, each of which is symmetrically  $n \times n$ , the mass matrix  $M$  being a positive definite matrix, the damping matrix  $C$  being a positive semi-definite matrix, and the stiffness matrix  $K$  being a positive definite matrix;

25  $P$  denotes an  $n \times p$  real matrix corresponding to positions of the actuators,

$x(t)$  and  $u(t)$  respectively denote  $n \times 1$  state and disturbance vectors;

$f(t)$  denotes a  $p \times 1$  external force vector;

$I$  is an  $n \times n$  unit matrix;

$S$  is a matrix consisting of eigenvectors of the stiffness matrix  $K$  and is normalized with respect to the mass matrix  $M$ ; and

$$Q = S^T P, \hat{f} = Qf(t), x(t) = S\xi(t), u(t) = S\eta(t),$$

$S^T K S = \text{diag}[\omega_i^2] = \Lambda_K$ , and  $S^T C S = \hat{C} = \text{diag}[2\zeta_i \omega_i]$  are satisfied by the matrix  $S$ .

11. A method for controlling a vehicle suspension system, the vehicle suspension including a plurality of dampers and a plurality of actuators, the vehicle suspension system being formalized by an equation (1) and being transformed to a decoupled equation (2), the method comprising:

calculating a velocity vector  $\dot{x}(t)$  of a state vector  $x(t)$  of equation 1;

calculating an actuating force  $f(t)$  such that the actuating force  $f(t)$

satisfies

$$\left\{ \begin{array}{ll} \text{if } Q_1 sign(\dot{\xi}_1) \geq 0 \& Q_2 sign(\dot{\xi}_2) \geq 0 \& \dots Q_n sign(\dot{\xi}_n) \geq 0, & f_j = -F_A \\ \text{if } Q_1 sign(\dot{\xi}_1) \geq 0 \& Q_2 sign(\dot{\xi}_2) \geq 0 \& \dots Q_n sign(\dot{\xi}_n) < 0, & f_j = -F_1 \\ \vdots & \vdots \\ \text{if } Q_1 sign(\dot{\xi}_1) < 0 \& Q_2 sign(\dot{\xi}_2) < 0 \& \dots Q_n sign(\dot{\xi}_n) \geq 0, & f_j = -F_{(2^n-2)} \\ \text{if } Q_1 sign(\dot{\xi}_1) < 0 \& Q_2 sign(\dot{\xi}_2) < 0 \& \dots Q_n sign(\dot{\xi}_n) < 0, & f_j = -F_B \end{array} \right\}$$

with respect to  $i = 1, \dots, n$  and  $j = 1, \dots, p$ ; and

actuating the actuators by the calculated actuating force  $f(t)$ ,

wherein:

$F_A$  is a value in a range of zero (0) to  $F_P$ ;

$F_B$  is a value in a range of zero (0) to  $F_N$ :

$F_k$  for  $k = 1, \dots, (2^n - 2)$  is a value between  $F_p$  and  $F_N$ .

$F_P$  and  $F_N$ , respectively denote a positive maximum force and a negative

maximum force that a j-th actuator can generate;

equation (1) is

$$M\ddot{x}(t) + C(\dot{x}(t) - \dot{u}(t)) + K(x(t) - u(t)) = Pf(t); \text{ and}$$

equation (2) is

$$I\ddot{\xi}(t) + \text{diag}[2\zeta_i \omega_i] (\dot{\xi}(t) - \dot{\eta}(t)) + \Lambda_K (\xi(t) - \eta(t)) = \hat{f}(t)$$

wherein:

n and p respectively denote the degrees of freedom of the suspension system and the number of independent actuators;

$M$ ,  $C$ , and  $K$  respectively denote a mass matrix, a damping matrix, and a stiffness matrix, each of which is symmetrically  $n \times n$ , the mass matrix  $M$  being a positive definite matrix, the damping matrix  $C$  being a positive semi-definite matrix, and the stiffness matrix  $K$  being a positive definite matrix;

$P$  denotes an  $n \times p$  real matrix corresponding to positions of the actuators,

$x(t)$  and  $u(t)$  respectively denote  $n \times 1$  state and disturbance vectors;

$f(t)$  denotes a  $p \times 1$  external force vector;

$I$  is an  $n \times n$  unit matrix;

$S$  is a matrix consisting of eigenvectors of the stiffness matrix  $K$  and is normalized with respect to the mass matrix  $M$ ; and

$$Q = S^T P, \hat{f} = Qf(t), x(t) = S\xi(t), u(t) = S\eta(t),$$

$S^T K S = \text{diag}[\omega_i^2] = \Lambda_K$ , and  $S^T C S = \hat{C} = \text{diag}[2\zeta_i \omega_i]$  are satisfied by the matrix  $S$ .

12. The method of claim 11, wherein the actuating force  $f(t)$  satisfies

$$\begin{cases} \text{if } Q_{ij} \text{sign}(\dot{\xi}_i) \geq 0 \text{ for } i = 1, \dots, n, \quad f_j = -F_A \\ \text{if } Q_{ij} \text{sign}(\dot{\xi}_i) < 0 \text{ for } i = 1, \dots, n, \quad f_j = -F_B \\ \text{Otherwise,} \quad \quad \quad f_j = 0 \end{cases}$$

with respect to  $i = 1, \dots, n$  and  $j = 1, \dots, p$ .

13. The method of claim 12, wherein values of  $F_A$  and  $F_P$  are equal, and values of  $F_B$  and  $F_N$  are equal.